Coordinate Geometry

Distance formula

The distance between the points P (x_1, y_1) and Q (x_2, y_2) is given by PQ=x2-x12+y2-y12

Example 1:

Find the values of l, if the distance between the points (-5, 3) and (l, 6) is 5 units.

Solution:

The given points are A (-5, 3) and B (l, 6).

It is given that AB = 5 units

By distance formula we have

 λ --52+6-32=5 \Rightarrow λ +52+9=25 \Rightarrow λ 2+25+10 λ +9=25 \Rightarrow λ 2+10 λ +9=0 \Rightarrow λ +9 λ +1=0 \Rightarrow λ =-1, or λ =-9 Required values of l are -1 or -9.

- The distance of a point (x, y) from the origin O (0, 0) is given by OP=x2+y2.
- Section formula:

The co-ordinates of the point P (x,y), which divides the line segment joining the points A (x_1, y_1) and B (x_2, y_2) internally in the ratio m:n, are given by:

P x, y=mx2+nx1m+n, my2+ny1m+n

Example: In what ratio does the point (-4, 7) divide the line segment joining the points P (-1, 1) and Q (-6, 11).

Solution: Let the point (-4, 7) divide the line segment joining the points P (-1, 1) and Q(-6, 11) in the ratio λ : 1.

Thus, by section formula, we have:

$$-6\lambda+-1\lambda+1,11\lambda+1\lambda+1=-4,7\Rightarrow-6\lambda-1\lambda+1=-4,11\lambda+1\lambda+1=7\Rightarrow-6\lambda-1=-4\lambda-4\Rightarrow2\lambda=3\Rightarrow\lambda=32$$

Therefore, the required ratio is 3:2.

• The **mid-point** of the line segment joining the points A (x_1, y_1) and B (x_2, y_2) is x1+x22, y1+y22. [Note: Here, m = n = 1]

- If A (x_1, y_1) , B (x_2, y_2) and C (x_3, y_3) are the vertices of \triangle ABC, then the coordinates of its **centroid** are given by the point x1+x2+x33, y1+y2+y33.
- Area of a triangle







The area of a triangle whose vertices are (x_1, y_1) , (x_2, y_2) and (x_3, y_3) is given by the numerical value of the expression 12x1y2-y3+x2y3-y1+x3y1-y2

Example 1:

Find the area of the triangle whose vertices are P(-2, 2), Q(2, 0) and R(8, 5).

Solution:

We have P(-2, 2), Q(2, 0) and R(8, 5) as the given points.

Let
$$(x_1, y_1) = (-2, 2)$$
; $(x_2, y_2) = (2, 0)$; $(x_3, y_3) = (8, 5)$ area of $\triangle PQR = 12x1y2-y3+x2y3-y1+x3y1-y2 \Rightarrow$ area of $\triangle PQR = 12-20-5+25-2+82-$

0⇒area of $\triangle PQR = 1210+6+16$ ⇒area of $\triangle PQR = 12\times32$ ⇒area of $\triangle PQR=16$ squ are units

Example 2:

If the points (-4, 1), (2, 4) and (p, 6) are collinear, then find the value of p.

Solution:

Since (-4, 1), (2, 4), (p, 6) are collinear, the area of the triangle formed by these points is zero.

 $\therefore 12-44-6+26-1+p1-4=0 \Rightarrow 8+10-3p=0 \Rightarrow 18-3p=0 \Rightarrow 3p=18 \Rightarrow p=183 \Rightarrow p=6$





